

UNIVERSIDADE FEDERAL DE LAVRAS
PRÓ-REITORIA DE PÓS-GRADUAÇÃO
COORDENADORIA DE PÓS-GRADUAÇÃO *STRICTO SENSU*

DISCIPLINA

Código	Denominação	Crédito(s) (*)	Carga Horária		
			Teórica	Prática	Total
	Linear and Integer Programming	4	60	0	60
DEPARTAMENTO		PROFESSOR(ES)			
Departamento de Ciência da Computação (DCC)		Dilson Lucas Pereira Mayron César de Oliveira Moreira			

EMENTA: (Síntese do Conteúdo)

Linear programming. Graphical solution of linear programs. Linear algebra and convex analysis. The Simplex Method. Duality and sensitivity analysis. Mixed-Integer programming. Relaxations and bounds. Well solved problems. Branch-and-Bound. Cutting planes.

(*) 15 horas/aulas teóricas = 1 crédito
15 horas/aulas práticas = 1 crédito

ASSINATURA(S): _____

Aprovado na Assembléia Departamental em _____ / _____ / _____

_____ - Chefe do Departamento

Lavras, _____ / _____ / _____

CONTEÚDO PROGRAMÁTICO

1. Linear Programming

- 1.1. The Linear Program
- 1.2. Linearity hypotheses: additivity, proportionality, divisibility and certainty
- 1.3. Classic formulations: the diet problem, the transportation problem, production planning problems, cutting and packing problems

2. Graphical solution of linear programs

- 2.1. Drawing two dimension feasible search regions (polytope)
- 2.2. Characterizing feasible regions
- 2.3. Finding optimal solutions by analysis of the gradient vector and function level curves

3. Linear Algebra and Convex analysis

- 3.1. Vectors and Matrices
- 3.2. Convex sets and convex functions
- 3.3. Polyhedral sets and cones
- 3.4. Extreme points, directions, extreme directions, faces
- 3.5. General representation theorem

4. The Simplex Method

- 4.1. Extreme points and optimality
- 4.2. Basic feasible solutions
- 4.3. The Simplex Method
- 4.4. Two-phase method
- 4.5. Big-M method
- 4.6. The Simplex Method in tableau format

5. Duality and Sensitivity Analysis

- 5.1. The Dual Problem
- 5.2. Primal-Dual relationships
- 5.3. Sensitivity analysis
- 5.4. The Dual Simplex Method

6. Mixed-Integer Programming

- 6.1. The Mixed-Integer Program
- 6.2. Classic formulations: The assignment problem, the knapsack problem, the set covering problem, the traveling salesman problem
- 6.3. Alternative, good and ideal formulations

7. Relaxations and bounds

- 7.1. Optimality and relaxations
- 7.2. The linear programming relaxation
- 7.3. Combinatorial relaxations
- 7.4. Lagrangian relaxation
- 7.5. Upper bounds

8. Well solved problems

- 8.1. Easy problems
- 8.2. Properties of easy problems
- 8.3. Dynamic programming
- 8.4. Complexity classes and reductions

9. Branch-and-bound

- 9.1. The branch-and-bound algorithm

10. Cutting planes

- 10.1. Valid inequalities
- 10.2. Gomory's Cuts
- 10.3. Mixed-Integer cuts

10.4. Other types of cuts

BIBLIOGRAFIA BÁSICA

Bazaraa, M., Jarvis, J. e Sherali, H., Linear Programming and Network Flows, 2nd edition, Wiley, 684 p., 1990.

Luenberger, D.G. e Ye, Y., Linear and nonlinear programming. Springer, 546 p., 2008.

Wolsey, L. A. Integer programming. John Wiley & Sons, 1998.

BIBLIOGRAFIA COMPLEMENTAR

Arenales, M. N., Armentano, V. A., Morabito, R. e Yanasse, H. H., Pesquisa Operacional, Editora Campus/Elsevier, 2ª edição, ISBN 85-352-1454-3, Rio de Janeiro, 2015, 723p.

Bertsimas, D. e Tsitsiklis, J.N., Introduction to linear optimization. Athena Scientific, 608p., 1997.

Chvatal, V., Linear Programming. W. H. Freeman, 478p. 1983.

Vanderbei, R. J., Linear Programming – Foundations and Extensions, Series: International Series in Operations Research & Management Science , Vol. 114, 464 p., 2008.

Computers & Industrial Engineering.

Computers & Operations Research.

European Journal of Operational Research.

International Journal of Production Research.

Journal of Heuristics.

Mathematical Programming.

Networks.

Omega.